

<u>EYFS</u>

Key Vocabulary: grouping, doubling, equal

| Objective & Strategy | Concrete | Pictorial | |
|---|--|--|-------------|
| -To be able to double numbers. -To experience equal groups of objects. | | <text><text><image/><image/></text></text> | A f calc |
| | Children will experience and explore equal groups of objects. Children will be encouraged to count the groups, then count how many objects are in a group. E.g. $2 \times 4=$ | Children will have images of equal groups to solve simple multiplication sentences by counting how many are in each equal group. | |
| | Double Physical and real-life examples that encourage children to see concept of doubling as adding two equal groups. | There are two groups. There are 4 teddies in each group. | |



Abstract

focus on symbols and numbers to form addition alculations to model adding two equal groups and doubles.

- 1 + 1 = 2
- 2 + 2 = 4
- 3 + 3 = 6
- 4 + 4 = 8
- 5 + 5 = 10



<u>Year 1</u>

Key Vocabulary: grouping, doubling, equal, groups of, lots of, times, array, altogether, multiply, count

| Objective & Strategy | Concrete | Pictorial | |
|--|---|--|----------------------|
| Objective & Strategy | Concrete | Fictorial | |
| -To count in steps of 2, 5 and 10s. | Children will be able to use concrete resources to count in steps of 2, 5 and 10. | Children will verbally say their number sequence aloud to demonstrate their understanding. Children would begin to count aloud and write numbers to match the sequence. E.g. 0, 5, 10, 15, 20 | Children Childrer |
| | | | |
| | Children will demonstrate knowledge of doubling through concrete resources. | Children will be able to use jottings and pictorial representations to show demonstration of doubling. Use the part whole method and bar models to show doubling alongside other picotrial representations. | Childrer ea |
| -To double numbers up to 20. | Double 5 equals 10 | | |
| | When beginning to double more complex numbers, children will need to explore partitioning the whole number into tens and ones, using base 10, and double the tens and then the ones, before recombining to find the total. | Double 16 equals 32 | |



Abstract

en will be able to count aloud in sequences, starting at different points.

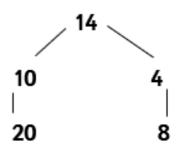
en will be able to write sequences with multiples of numbers

2, 4, 6, 8...

10, 20, 30, 40...

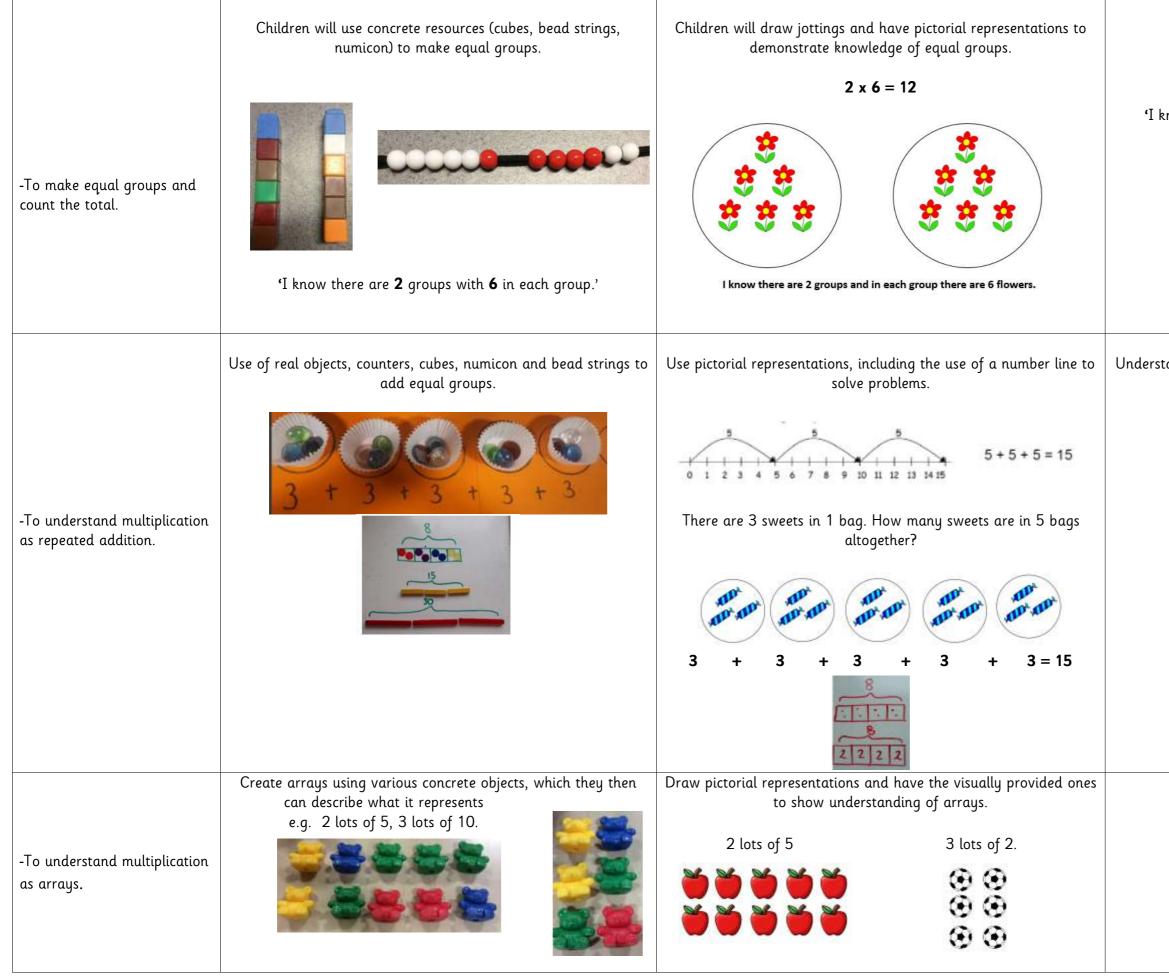
5, 10, 15, 20, 25, 30...

en will learn to partition a number and then double each part before recombining it back together.



20 + 8 = 28







Understand as a written calculation

$2 \times 6 = 12$

'I know there are **2** groups with **6** in each group.'

Understand and write repeated addition number sentences to describe pictures or objects.

3 + 3 + 3 + 3 + 3 = 15

Understand as a written calculation

 $2 \times 5 = 10$

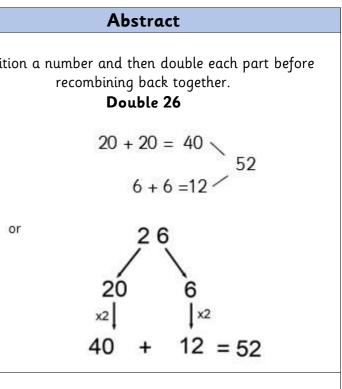


<u>Year 2</u>

Key Vocabulary: grouping, doubling, equal, groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, commutative law, inverse, sets of, lots of, equal groups, times, times as big as, once, twice, three times...

| Objective & Strategy | Concrete | Pictorial | |
|---|--|---|----------------------|
| | Use concrete apparatus base 10, place value counters or numicon to represent the numbers. Use base 10 or place value counters to partition a number before doubling. Double the ones then tens and recombine. | Use pictorial representations to show how to double numbers. Double 26 is 52 | Partitio |
| -To double numbers up to 100. | Double 26 is 52 | | 10 |
| | Use concrete appartus (counrters, cubes, bead strings) to show the groups. Count the groups; as children are skip counting, children may use their fingers as they are skip counting. Also use bar models. | Use a variety of pictorial representations to show representation of counting in multiples. | Write sequ |
| | 5 + 5 + 5 + 5 + 5 + 5 + 5 = 40 | and and and and and and | 0, 2, 4, 0, 3, 6, |
| -To count in multiples of 2s, 3s, 5s and 10s (repeated addition). | | | 0, 5, 10 |
| | 333 355 565 ? | 0 5 10 15 20 25 30 $0 4 x 2 =$ | 4 x 3 = 3 |
| | | ? 3 3 3 3 3 ^{5x3=} | |
| | | | |



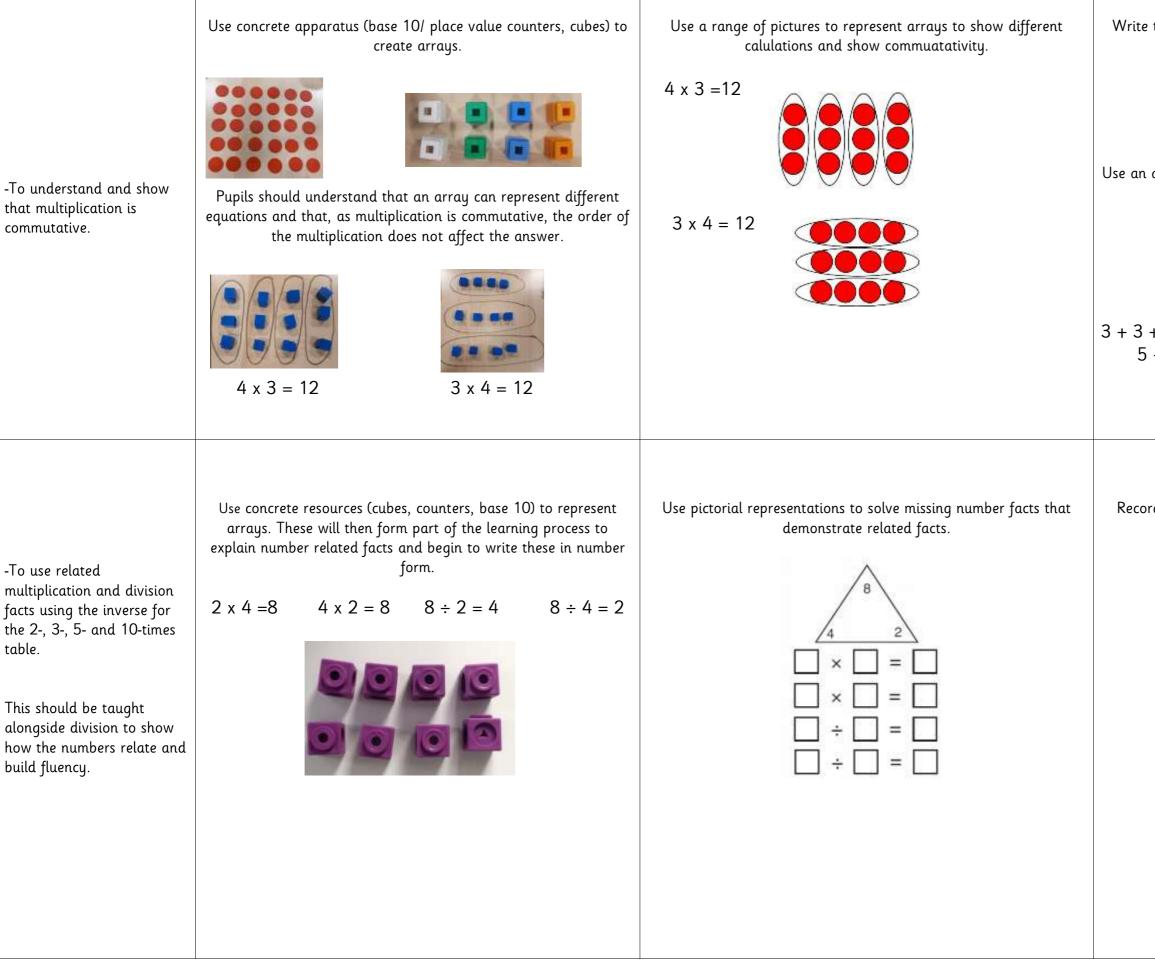


Count in multiples of a number aloud.

equences with multiples of numbers.

- i, 6, 8, 10
- 6, 9, 12, 15
- 0, 15, 20, 25, 30
- = 3 + 3 + 3 + 3 =

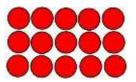






Write the different multiplication sentences to show the commutative law.

Use an array to write multiplication number sentences and reinforce repeated addition.



3 + 3 + 3 + 3 + 3 = 15 5 + 5 + 5 = 15

| 5 | х | 3 | = | 15 |
|---|---|---|---|----|
| 3 | х | 5 | = | 15 |

Record all 8 related number sentences to demonstrate related facts.

$$2 \times 4 = 8$$

 $4 \times 2 = 8$
 $8 \div 2 = 4$
 $8 \div 4 = 2$
 $8 = 2 \times 4$
 $8 = 4 \times 2$
 $2 = 8 \div 4$
 $4 = 8 \div 2$



<u>Year 3</u>

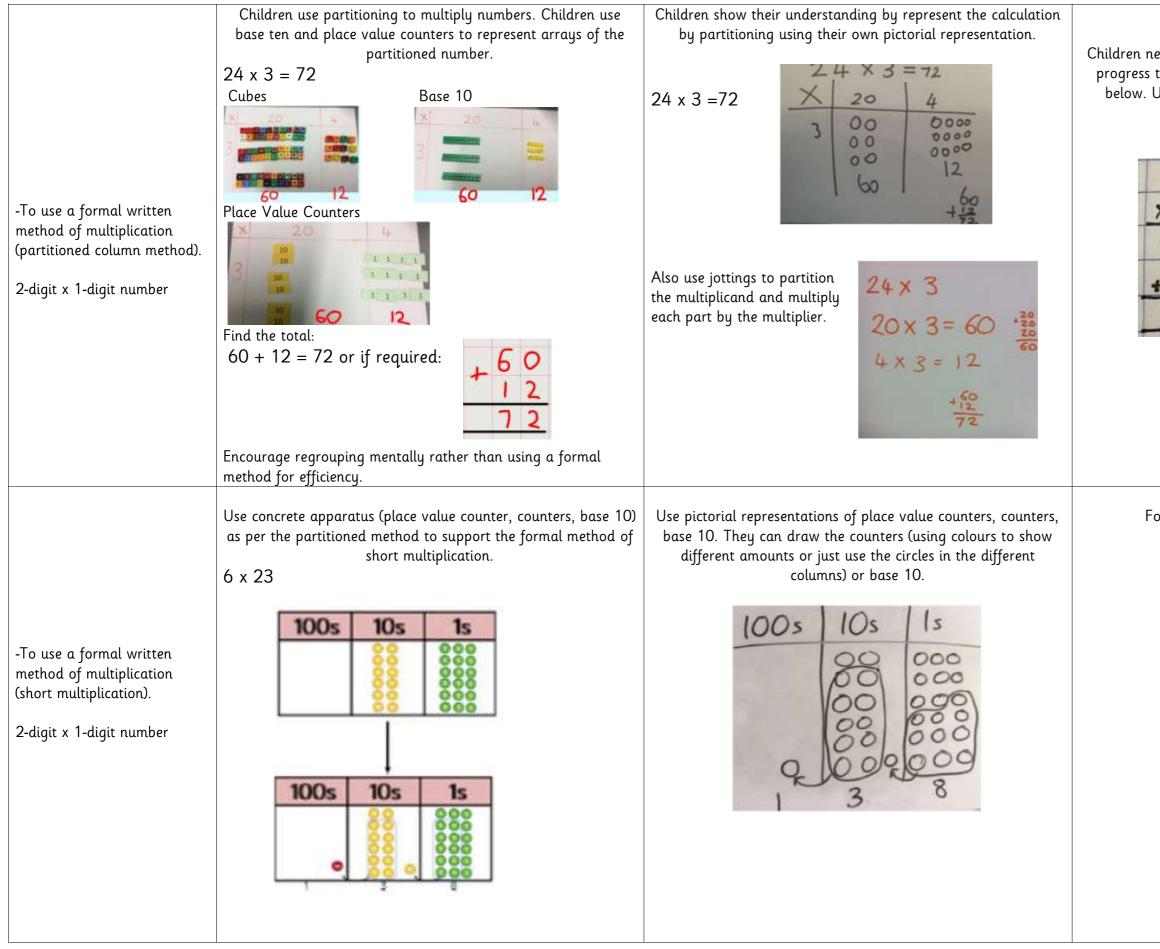
Key Vocabulary: grouping, doubling, equal, groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, commutative law, inverse, sets of, lots of, equal groups, times, times as big as, once, twice, three times..., partition, grid method, total, multiple, product, tens, ones, value

| Objective & Strategy | Concrete | Pictorial | Abstract |
|--|---|---|--|
| -To use related multiplication and division facts using the inverse for the 2-, 3-, 4-, 5-, 8- and 10- times table. | Use concrete apparatus (base 10, counters, cubes) to understand the link between multiplication and division and to find related facts. $3 \times 6 = 18 18 \div 3 = 6 \qquad 6 \times 3 = 18 18 \div 6 = 3$ | Use pictorial representations to show an array pictorially then find the associated multiplication and division facts by sorting into equal groups. 18, 2, 3, 4, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5, 5, | Apply understanding of inverse relationships to write related multiplication and division statements. $3 \times 6 = 18$ $6 \times 3 = 18$ $18 = 3 \times 6$ $6 \times 3 = 18$ $18 = 6 \times 3$ $18 \div 3 = 6$ $6 = 18 \div 3$ $18 \div 6 = 3$ $3 = 18 \div 6$ Use associated vocabulary correctly and know what each number represents in the calculation. multiplier multiplicand product $3 \times 6 = 18$ $18 \div 3 = 6$ $18 \div 3 = 6$ |
| -To use partitioning to support multiplication calculations. | Use concrete apparatus (place value counter, counters, base 10) to introduce the partitioned method by using arrays to demonstrate the links. 23 x 8 = 184 $10 \ 10 \ 1 \ 1 \ 1$ $10 \ 10 \ 1 \ 1 \ 1$ $160 \ + 24 \ = 184$ | Use pictorial representations of place value counters, counters, base 10. They can draw the counters (using colours to show different amounts or just use the circles in the different columns) or base 10. 14×4 00000 0000 00000 (0×4) 40 + 16 = 56 | Start with multiplying by one-digit numbers using partitioning, showing the clear addition. 14 x 6 (10 x 6) + (4 x 6) 60 + 24 = 84 |











Formal written partitioned method:

Children need to be secure with partitioning and related facts progress to the abstract method with regrouping as shown below. Use concrete apparatus alongside as a support if required.

× 3 × 3 2 × 3 0

Formal written short multiplication method:

6 x 23 = <u>6</u> 38 1 1



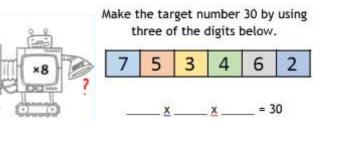
<u>Year 4</u>

Key Vocabulary: grouping, doubling, equal, groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, commutative law, inverse, sets of, lots of, equal groups, times, times as big as, once, twice, three times..., partition, grid method, total, multiple, product, tens, ones, value, hundreds, thousands, factor

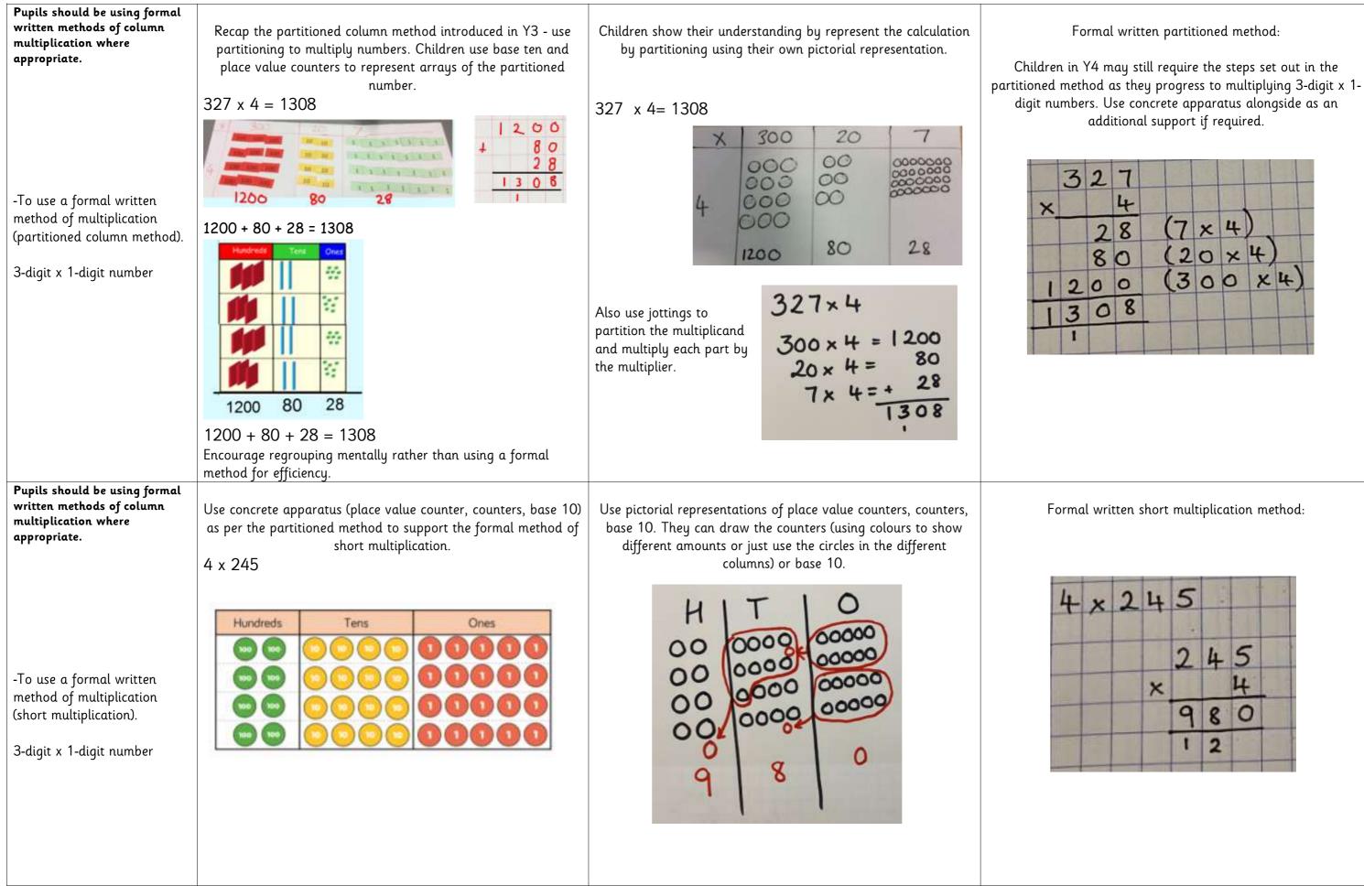
| Objective & Strategy | Concrete | Pictorial | Abstract |
|---|---|--|--|
| | Use concrete apparatus (base 10, counters, cubes) to understand the link between multiplication and division and to find related facts. | Use pictorial representations to show an array pictorially then find the associated multiplication and division facts by sorting into equal groups. | Apply understanding of inverse relationships to write related multiplication and division statements. $3 \times 6 = 18$ $18 = 3 \times 6$ $6 \times 3 = 18$ $18 = 6 \times 3$ $18 \div 3 = 6$ $6 = 18 \div 3$ |
| -To recall multiplication and division facts for multiplication tables up to 12x 12. | $3 \times 6 = 18$ $18 \div 3 = 6$ $6 \times 3 = 18$ $18 \div 6 = 3$ | $18 \div 3 = 6$ $18 \div 6 = 3$ | $18 \div 6 = 3$ $3 = 18 \div 6$ Use associated vocabulary correctly and know what each number represents in the calculation. |
| | | 3×6=18 6×3=18 | multipliermultiplicandproductdividenddivisorquotient $3 \times 6 = 18$ $18 \div 3 = 6$ 7111numbernumber innumbernumbernumberof groupseach groupin allin allof groups |
| | Multiply and divide numbers by zero and one. Understand the meaning of the calculation and the need of equal sized groups. | Show understanding of multiplying by 0 and 1 by drawing representations. | Understand how to multiply by 1 and 0 and apply to word problems. 1 x 83 = 76 x 1 = 4567 x 0= 0 x 23 = |
| | $6 \times 2 = 12$ $6 \times 1 = 6$ $6 \times 0 = 0$ | $4x0=0 4x1=4 \\ \bigcirc $ | Jack earns £12 a week on his paper round. He did not work for one week whilst he was on holiday. How |
| -To multiply and divide mentally, including: multiplying by 0 and 1 and multiplying together 3 numbers. | Use objects to calculate totals when three numbers are multiplied together. 2 x 4 x 5 = 40 | Use objects to calculate totals when three numbers are multiplied together. $2 \times 4 \times 5 = 40$ $2 \times 4 \times 5 = 40$ $2 \times 4 \times 5 = 20$ $2 \times 4 \times 5 = 20$ $3 \times 4 \times 5 = 20$ $3 \times 4 \times 5 = 40$ Or may be represented as: $2 \times (4 \times 5)$ $2 \times (20) = 40$ | much did he earn?Solve number puzzles using the knowledge of multiplying 3 single digit numbers.Make the target number 30 by using three of the digits below. $7 5 3 4 6 2$ $x - x - 30$ |















<u>Years 5</u>

Key Vocabulary: grouping, doubling, equal, groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, commutative law, inverse, sets of, lots of, equal groups, times, times as big as, once, twice, three times..., partition, grid method, total, multiple, product, tens, ones, value, hundreds, thousands, factor, square, cube, integer, decimal, short multiplication, long multiplication, 'carry', composite numbers, prime numbers, prime factors

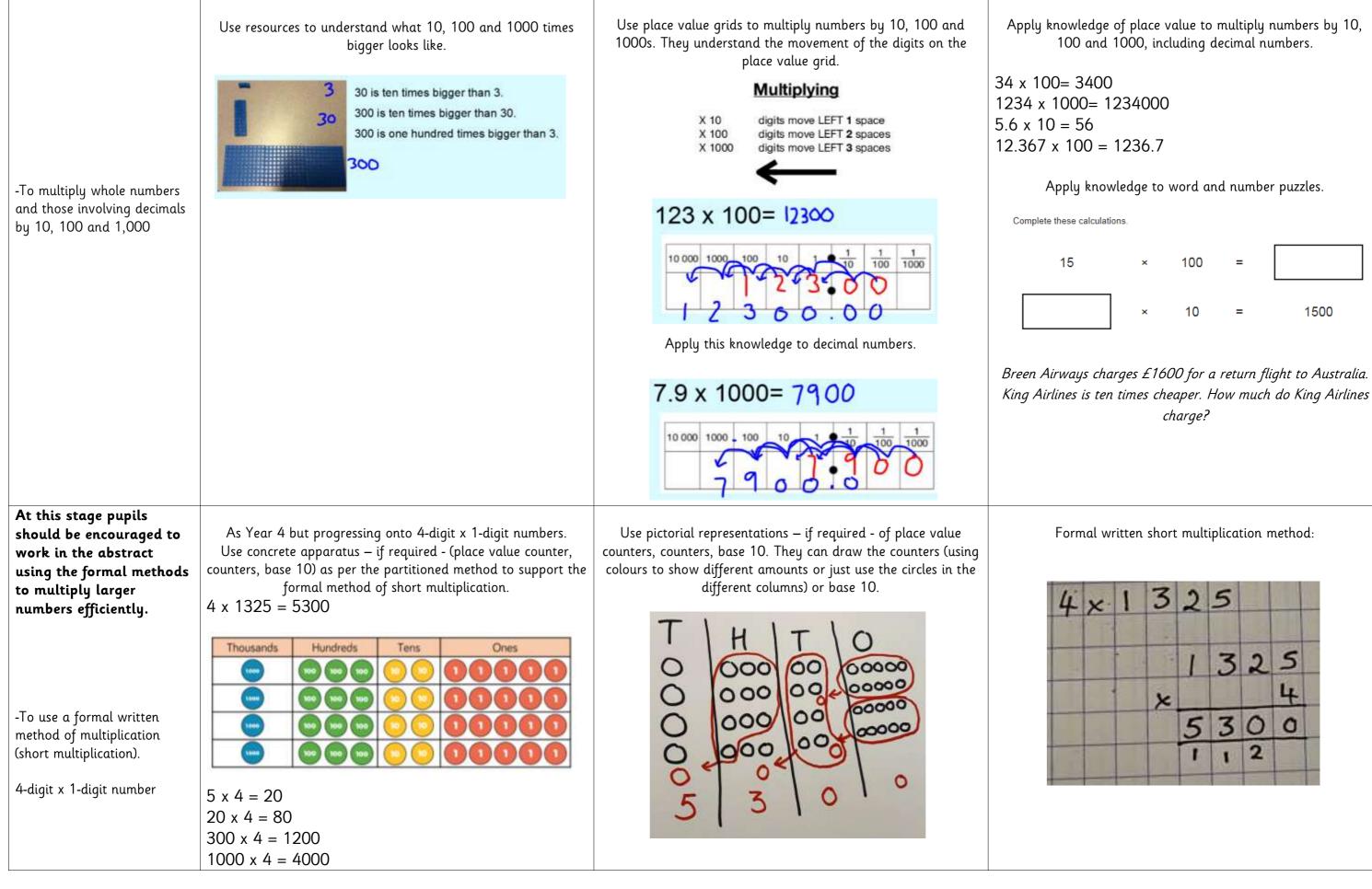
| Objective & Strategy | Concrete | Pictorial | Abstract |
|---|--|---|---|
| -To recall multiplication and division facts for multiplication tables up to 12x 12. | Use concrete apparatus (base 10, counters, cubes) to understand the link between multiplication and division and to find related facts. $3 \times 6 = 18$ $18 \div 3 = 6$ $6 \times 3 = 18$ $18 \div 6 = 3$ | Use pictorial representations to show an array pictorially then find the associated multiplication and division facts by sorting into equal groups. $18 \div 3 = 6$ $3 \times 6 = 18$ $3 \times 6 = 18$ $18 \div 6 = 3$ $6 \times 3 = 18$ | Apply understanding of inverse relationships to write related multiplication and division statements. $3 \times 6 = 18$ $6 \times 3 = 18$ $18 = 3 \times 6$ $6 \times 3 = 18$ $18 = 6 \times 3$ $18 \div 3 = 6$ $18 \div 6 = 3$ $18 \div 6$ Use associated vocabulary correctly and know what each number represents in the calculation. multiplier multiplicand product $3 \times 6 = 18$ $18 \div 3 = 6$ $18 \div 3 = 6$ |
| -To recognise and use square numbers and cube numbers. | <image/> Use resources to explore squared and cubed numbers. Square numbers 4 9 16 Cubed numbers 8 27 | Represent squared and cubed numbers pictorially. They use the correct notation for squared (2) and cubed (3). $ \begin{array}{c} 2^{2} \\ \frac{2}{1 \ 2} \\ \frac{3}{4 \ 5 \ 6} \\ \frac{1}{2 \ 3} \\ 2x2 = 4 \\ 3x3 = 9 \\ 4x4 = 16 \\ \end{array} $ | Find and recognise squared and cubed numbers and use the correct notation for squared (2) and cubed (3). $2^{2} \text{ or } 2 \times 2 = 4$ $3^{2} \text{ or } 3 \times 3 = 9$ $4^{2} \text{ or } 4 \times 4 = 16$ $1^{3} = 1 \times 1 \times 1 = 1$ $2^{3} = 2 \times 2 \times 2 = 8$ $3^{3} = 3 \times 3 \times 3 = 27$ $4^{3} = 4 \times 4 \times 4 = 64$ |



$$2^{2} \text{ or } 2 \times 2 = 4$$

 $3^{2} \text{ or } 3 \times 3 = 9$
 $4^{2} \text{ or } 4 \times 4 = 16$
 $1^{3} = 1 \times 1 \times 1 = 1$
 $2^{3} = 2 \times 2 \times 2 = 8$
 $3^{3} = 3 \times 3 \times 3 = 27$
 $4^{3} = 4 \times 4 \times 4 = 64$

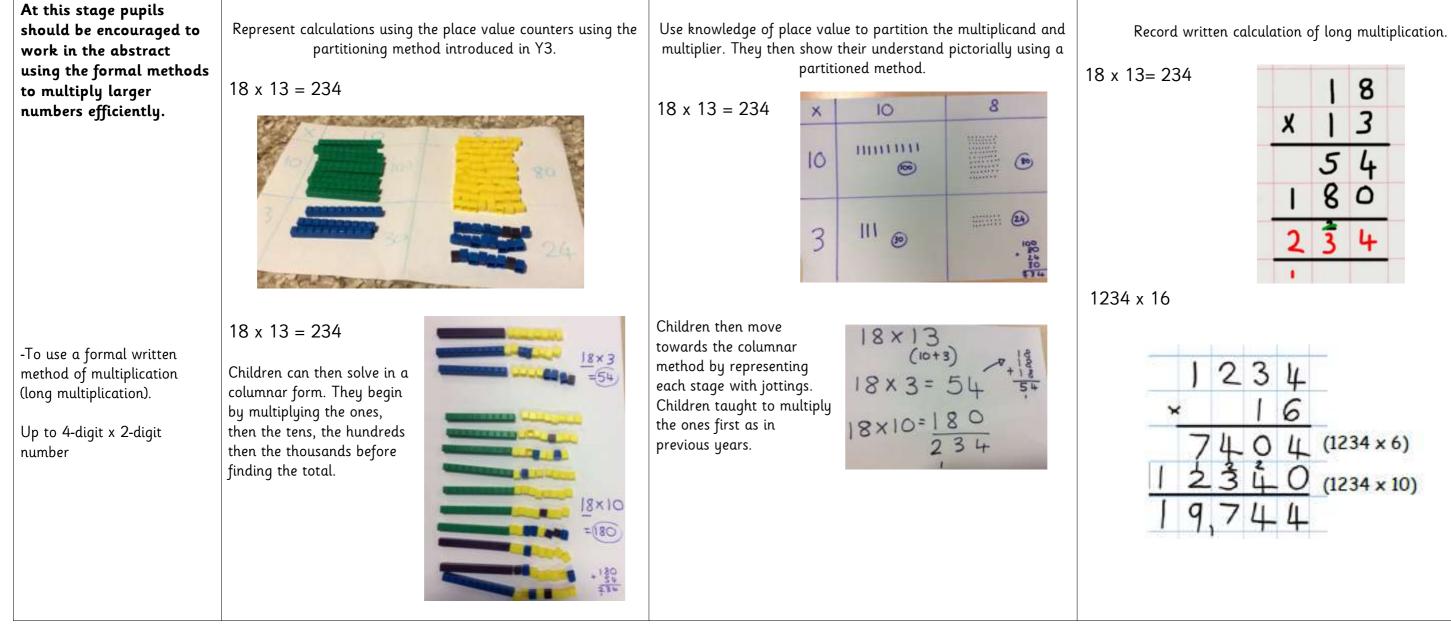




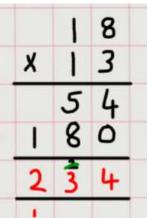


| 15 | × | 100 | = | |
|----|---|-----|---|------|
| | × | 10 | = | 1500 |











<u>Years 6</u>

Key Vocabulary: grouping, doubling, equal, groups of, lots of, times, array, altogether, multiply, count, multiplied by, repeated addition, column, row, commutative law, inverse, sets of, lots of, equal groups, times, times as big as, once, twice, three times..., partition, grid method, total, multiple, product, tens, ones, value, hundreds, thousands, factor, square, cube, integer, decimal, short multiplication, long multiplication, 'carry', composite numbers, prime numbers, prime factors

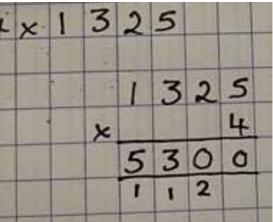
| Objective & Strategy | Concrete | Pictorial | Abstract |
|---|--|---|--|
| At this stage pupils should be encouraged to work in the abstract. | Use concrete apparatus (base 10, counters, cubes) to understand the link between multiplication and division and to find related facts. | Use pictorial representations to show an array pictorially then find the associated multiplication and division facts by sorting into equal groups. | Apply understanding of inverse relationships to write related multiplication and division statements. $3 \times 6 = 18$ $18 = 3 \times 6$ $6 \times 3 = 18$ $18 = 6 \times 3$ |
| -To recall multiplication and division facts for multiplication tables up to 12x 12. | $3 \times 6 = 18$ $18 \div 3 = 6$ $6 \times 3 = 18$ $18 \div 6 = 3$ | $ \begin{array}{c} 18 \div 3 = 6 \\ 3 \times 6 = 18 \end{array} $ | $18 \div 3 = 6 \qquad 6 = 18 \div 3$ $18 \div 6 = 3 \qquad 3 = 18 \div 6$ Use associated vocabulary correctly and know what each number represents in the calculation. $\begin{array}{c} \text{muttiplier multiplicand product} & \text{dividend divisor quotient} \\ 3 \times 6 = 18 & 18 \div 3 = 6 \\ 7 & 1 & 1 \\ 10 & \text{mutter in number number number number number in of groups each group in all in all of groups each group} \end{array}$ |
| At this stage pupils should be encouraged to work in the abstract. | Use resources to understand what 10, 100 and 1000 times bigger looks like. 30 is ten times bigger than 3. 300 is ten times bigger than 30. 300 is one hundred times bigger than 3. | Use place value grids to multiply numbers by 10, 100 and 1000s. They understand the movement of the digits on the place value grid. Multiplying X 10 digits move LEFT 1 space X 100 digits move LEFT 2 spaces | Apply knowledge of place value to multiply numbers by 10, 100 and 1000, including decimal numbers. 34 x 100= 3400 1234 x 1000= 1234000 5.6 x 10 = 56 |
| -To multiply whole numbers and those involving decimals by 10, 100 and 1,000 | 300 | X 1000 digits move LEFT 3 spaces 123 x 100= 12300 10 000 100 10 10 1 10 1 100 1000 1 2 3 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 | 12.367 x 100 = 1236.7 Apply knowledge to word and number puzzles. Here are five number cards 0.47 10 100 1000 4.07 Use four of the cards to complete these calculations. |
| | | Apply this knowledge to decimal numbers. | 47 ÷ [] = [] |
| | | 7.9 x 1000= 7900 $10\ 000\ 100\ 100\ 10\ 10\ 10\ 10\ 10\ 1$ | × = 40.7 |

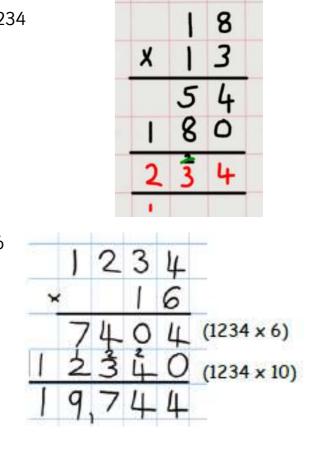




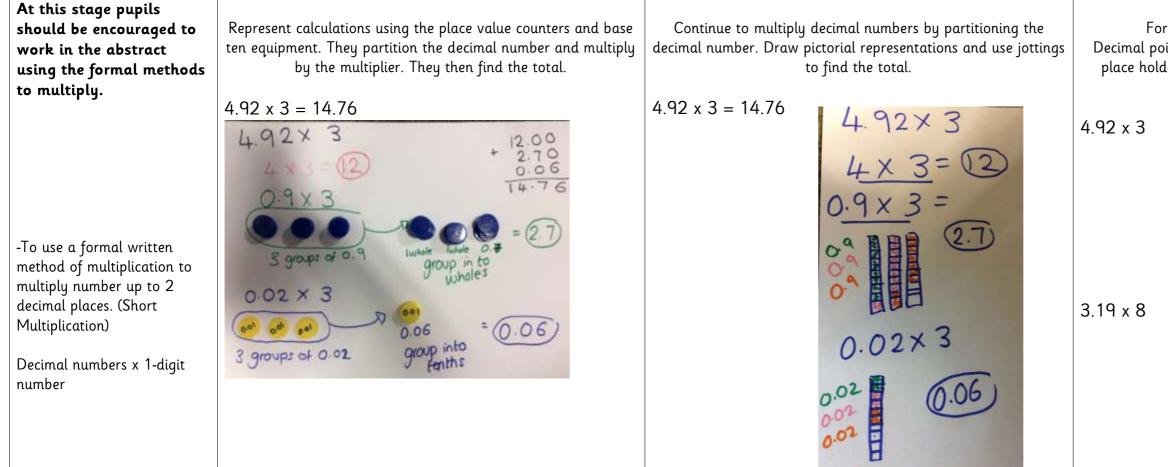
At this stage pupils As Year 4 but progressing onto 4-digit x 1-digit numbers. Use pictorial representations – if required - of place value Formal written short multiplication method: should be encouraged to Use concrete apparatus – if required - (place value counter, counters, counters, base 10. They can draw the counters (using work in the abstract counters, base 10) as per the partitioned method to support the colours to show different amounts or just use the circles in the using the formal methods formal method of short multiplication. different columns) or base 10. to multiply larger 32 5 4× 4 x 1325 = 5300 numbers efficiently. Thousands Ones Hundreds Tens 3 2 5 000 60 60000 \circ 00000 00 000 0000 1000 × 00000 000 -To use a formal written 00 5 30 1000 0 20000 method of multiplication 000 1 2 (short multiplication). 0 0 4-digit x 1-digit number $5 \times 4 = 20$ 20 x 4 = 80 $300 \times 4 = 1200$ $1000 \times 4 = 4000$ At this stage pupils Represent calculations using the place value counters using the Use knowledge of place value to partition the multiplicand and should be encouraged to Record written calculation of long multiplication. partitioning method introduced in Y3. multiplier. They then show their understand pictorially using a work in the abstract partitioned method. using the formal methods 18 x 13= 234 8 18 x 13 = 234 to multiply larger 8 18 x 13 = 234 × 10 3 numbers efficiently. X 11111111111 5 10 10 6 ٥ 2 111 3 (30) -To use a formal written method of multiplication $18 \times 13 = 234$ 1234 x 16 (long multiplication). 23 Children can then solve in a Children then move 18×13 Up to 4-digit x 2-digit columnar form. They begin towards the columnar (10+3 number by multiplying the ones, method by representing then the tens, the hundreds each stage with jottings. then the thousands before Children taught to multiply the ones first as in finding the total. 8×10= previous years. 18×10 =180













Formal written short multiplication method: Decimal points line up under each other, zeros are added at place holders and the multiplier must be positioned in the correct place value column.

